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#### Abstract

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## ABSTRACT

The estimation of the population size of animals has long been a difficult work. The catch-depletion method, a method based on the catch effort and the catch numbers, has been widely used, especially in estimating the fish density in streams. Limited by the investment of time and labor, most field measures use two-catch or three-catch method, which may lead to the inaccurate measurement. Here we investigated how the number of catching rounds and the capture probability influence the accuracy of the estimates of catch-depletion method. We found that ...

## KEYWORDS : -population size, maximum likelihood, catch-depletion method

## INTRODUCTION

Measuring the precise estimates of animal abundance has long been a central and challenge topic for ecologists (Lockwood \& Schneider 2000). The methods could be divided into two categories: mark-recapture experiments and catch-depletion method (Seber \& Le Cren 1967). The former one is suitable for the terrestrial animals like mice and moose, which can be relatively easy to be marked. The latter method has been widely used in estimating fish density in streams, small rivers or ponds (Peterson et al. 2004), where capture by electricity is easy.

The catch-depletion method estimates the fish density by analyzing the catch effort, i.e. the number of caught fish. Fish is caught by electric equipment in net-enclosed water body (Bacon \& Youngson 2007). Restricted by the investment of time and labor, usually two or three rounds are used. However, this might causes the inaccuracy of estimates (Peterson et al. 2004). Here we calculated the fish abundance estimates of catch-depletion method with different number of rounds under different capture probability. The aim is to investigate the influence of the round numbers and the capture probability on the accuracy of the catch-depletion method.

## MATERIALS AND METHODS

## Likelihood function

Define $N$ as the number of individuals before fishing, $Z_{i}$ as the catch effort by round $i$, and $p$ as the probability that any one fish is caught. The probability that the catch in first round is exactly $Z_{i}$ is given by

$$
\begin{equation*}
P\left(Z_{1}\right)=C_{N}^{z_{i}} p^{z_{i}}(1-p)^{N-z_{i}}=\frac{N!}{Z_{1}!\left(N-Z_{1}\right)!} p^{z_{i}}(1-p)^{N-z_{i}} \tag{1}
\end{equation*}
$$

For two-catch method, the joint probability of $Z_{1}$ and $Z_{2}$ is given by

$$
\begin{equation*}
P\left(Z_{1}, Z_{2}\right)=\frac{N!}{Z_{1}!Z_{2}!\left(N-Z_{1}-Z_{2}\right)!} p^{z_{1}+z_{2}}(1-p)^{N-z_{i}+N-z_{1}-z_{2}} \tag{2}
\end{equation*}
$$

Then for all the $n$ rounds, the joint probability distribution of $Z_{1}, Z_{2_{\text {a }}, \ldots e}$ and $Z_{m m}$ is given by

$$
\begin{equation*}
P\left(Z_{1}, Z_{2}, \ldots, Z_{n}\right)=\frac{N!}{\prod_{i=1}^{n} Z_{i}!\left(N-\sum_{i=1}^{n} Z_{i}\right)!} p^{\sum_{\alpha}^{*} z_{i}}(1-p)^{\sum_{x}^{n}\left(N-\sum_{\alpha}^{i} z_{i}\right)} \tag{3}
\end{equation*}
$$

$+\sum_{i=1}^{n}\left(N-\sum_{j=1}^{i} Z_{j}\right) \log (1-p)$

In this function, $N$ and $p$ are unknown parameters, so we can write this
function as
$\log L_{n}=f(N, p)$

Artificial data and Maximum Likelihood Estimate (MLE)
We assumed the total number $(N)$ of fish in enclosed water body is 1,000 . Under different capture probability ( $p$ ), we calculated the supposed number for each round of catch (see Table 1). For each round under each capture probability, we calculated the MLE of the fish number ( $N^{*}$ ) and capture probability ( $p^{*}$ ). Then, we fixed $p^{*}$ and calculated the log-likelihood values for different fish number, and got the $95 \%$ confidence intervals $(95 \% \mathrm{Cl})$ of fish number using likeli-hood-ratio test (LRT).

Table 1 Artificial data which show the fish number for each round of catch under different capture probability.

| Index <br> of the <br> round <br> (i) | Assumed Capture probability (p) |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
|  | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |  |
| 1 | 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 |  |
| 2 | 90 | 160 | 210 | 240 | 250 | 240 | 210 | 160 | 90 |  |
| 3 | 81 | 128 | 147 | 144 | 125 | 96 | 63 | 32 | 9 |  |
| 4 | 73 | 102 | 103 | 86 | 63 | 38 | 19 | 6 | 1 |  |
| 5 | 66 | 82 | 72 | 52 | 31 | 15 | 6 | 1 | 0 |  |

## RESULTS AND DISCUSSION

We demonstrated an illustration of the likelihood-ratio test (Fig. 1), which showed that increasing the number of catch round from 2 to 5 could decrease the $95 \% \mathrm{Cl}$ dramatically from [965, 1036] to [990, 1011], which indicated the increasing accuracy of the estimates. Surprisingly increasing $n$ rarely altered the MLE of fish number.


Figure 1 Illustration of the likelihood-ratio test for the artificial data when assumed $p$ is 0.5 . Different colors indicate different nu mber of rounds. The horizontal line indicates the $95 \%$ range of the estimates.

## The extended

analyses for all the artificial data showed similar pattern (Table 2), i.e. increasing the number of rounds would shorten the $95 \% \mathrm{Cl}$, especially when the capture probability was small. Additionally, we also found the MLE of fish number might be underestimated when both round number and capture probability were small.

Table 2 The maximum likelihood estimate (MLE) and the $95 \%$ lower boundary (LB) and upper boundary (UB) of the fish numbers.

| Number of rounds (n) | Bounds and estimates | Assumed Capture probability (P) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.1 | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 | 0.7 | 0.8 | 0.9 |
| 2 | LB | 801 | 882 | 917 | 955 | 965 | 974 | 981 | 988 | 994 |
|  | MLE | 842 | 957 | 973 | 999 | 1000 | 999 | 1000 | 1000 | 1000 |
|  | UB | 952 | 1038 | 1033 | 1047 | 1036 | 1027 | 1019 | 1012 | 1006 |
| 3 | LB | 830 | 938 | 957 | 968 | 977 | 985 | 990 | 995 | 999 |
|  | MLE | 918 | 999 | 999 | 999 | 1000 | 999 | 1000 | 1000 | 1000 |
|  | UB | 1013 | 1064 | 1045 | 1033 | 1023 | 1016 | 1010 | 1005 | 1002 |
| 4 | LB | 918 | 949 | 966 | 976 | 985 | 990 | 995 | 998 | 1000 |
|  | MLE | 1000 | 999 | 1000 | 999 | 1000 | 999 | 1000 | 999 | 1000 |
|  | UB | 1088 | 1051 | 1035 | 1023 | 1016 | 1009 | 1005 | 1002 | 1000 |
| 5 | LB | 929 | 958 | 973 | 983 | 990 | 994 | 998 | 999 | 1000 |
|  | MLE | 1001 | 999 | 1000 | 999 | 1000 | 999 | 1000 | 999 | 1000 |
|  | UB | 1077 | 1043 | 1028 | 1017 | 1011 | 1005 | 1003 | 1000 | 1000 |

Increasing the capture probability would also decrease the standard error of the MLE (Fig. 2). If $p$ varied from 0.1 to 0.9 , the standard error could change from about 40 to around 5 . This indicates the importance of increasing the capture probability.


Figure 2 The relationship between the standard error of MLE and the captured probability. Different colors indicate different number of rounds.

## CONCLUSION

Our findings demonstrated that two or more rounds of catch with capture probability higher than 0.4 could make sure an accurate estimate of fish number. More rounds of catch or higher capture probability indeed shortened the confidence interval of the estimates, i.e. decreased the standard error.

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