# PROGRAMMATIC APPROACH FOR FINDING THE PROJECT DURATION AND ASSOCIATED COST 

## KEYWORDS

Project duration, Project cost, EST, EFT, LST, LFT and Slack.

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#### Abstract

This research paper provides an alternative approach for estimating the project duration and the associated cost by using C programming Language adopting mathematical representation. Project duration and cost play a prominent role in gratifying the cores of both the service provider and the client. A program is created for measuring the earliest starting time, earliest finishing time, latest starting time, latest finishing time and slack by taking input as normal time, crash time, normal cost and crash cost. The output is the objective of this paper, determining duration and the total cost of the project which condenses the time for project managers in decision making and project scheduling.


## 1.INTRODUCTION

J.E. Kelly of Remigton-Rand and M.B. Walker of Dupont developed CPM in 1950's to assist in scheduling maintenance shutdowns of chemical processing plants. Pert was developed shortly after by the U.S. Navy to manage the development of the Polaris missile [6].

Ameen [1] developed Computer Assisted PERT Simulation (CAPERTSIM), an instructional tool to teach project management techniques. Students used the program to evaluate decision-making under uncertainty and cost-time relationships.

The critical path method (CPM) and the program evaluation review technique (PERT), two management science techniques developed in the late 1950s to plan, schedule, and control large, complex projects with many activities. These approaches differ primarily on how the duration and the cost of activities are processed. A project network representation is taken in use to illustrate the project mode and its associations. A network consists of a set of circles recognized as nodes and line connecting nodes jointly recognized as arcs. Its familiar approaches of a project network representation are motion on node (AON) or motion on are (AOA). The node of the networks embodies the project motions and the arcs illustrate their prior relationships as the first approach. The next approach, the project activities are stated on arcs and nodes represent the starting or completion of activities. The immediate predecessors of an activity refer to those activities that must be completed prior to the starting time of a given activity. Similarly, immediate successors of an activity refer to those that follow the completion of a given activity [2].

The PERT method uses only the activity time means in calculating the critical path, reducing the stochastic model to a deterministic model. A single critical path is thus calculated and used, whereas in reality there may be numerous possible critical paths realized. For a large network the probability that any given path may be the critical one may be very small. As a result, the traditional PERT method of calculating the time to complete the project is almost always too low. The extent to which PERT underestimates completion times is examined for a variety of networks by Klingel (1966) [5].

Crowson proposed a modified CPM method that deteriorates a project network into sub - networks containing only specific nodes (the decision nodes) and the longest remoteness between them [3].

Program (Project) Evaluation and Review Technique (PERT) followed by CPM (Critical Path Method) is a method of modeling, testing, simulating and solving a wide range of simplex large range problems. The same technique is used in this project to determine the critical path and the expected duration of the bottling unit startup [8].

Critical path is the sequence of activities which add up to the longest overall duration. It is the shortest time possible to complete the project. Any delay of an activity on the critical path directly impacts the planned project completion date (there is no float on the critical path). A project can have several, parallel, near critical paths. An additional parallel path through the network with the total durations shorter than the critical path is called a sub-critical or non-critical path. The Critical Path Method or Critical Path Analysis is a mathematically based algorithm for scheduling a set of project activities. The essential technique for using CPM is to construct a model of the project that includes a list of all activities required to complete the project, the time (duration) that each activity will take to completion and the dependencies between the activities. CPM calculates the longest path of planned activities to the end of the project and the earliest and latest that each activity can start and finish without making the project longer and determines "critical" activities (on the longest path) [4].

Complex projects require a series of activities which must be performed sequentially. These activities can be modeled as a network. Completing a project on time and within budget is not an easy task. A project can be defined as a set of a large number of activities or jobs that are performed in a certain sequence determined logically or technologically and it has to be completed within a specified time and cost whilst meeting the performance standards[9]. Using input values such as activities normal time, crash time, normal cost and crash cost, the program are developed for computing slack value, estime, eftime, lstime and lftime by employing CPM techniques. Based on the slack value, which activity has critical path should be considered for evaluation. The cost of labouring and equipment materials everyday expenditure assigned in desiring the activity is the direct cost of labouring. The direct cost of an activity is the cost of labor and equipment employed in completing the activity.

The total cost of the project which is the aggregate summation of the direct project's activity costs and the indirect cost is multiplying with the total duration. On the other hand, the indirect cost will decline by decreasing the project duration, as the indirect cost are almost a linear function with the project duration [2]. Indirect project costs include general expenses that cannot directly be attributed to particular activities and exist regardless of activity progress. Indirect costs are typically assumed to be proportional to project duration [8]. Above mentioned manner, the problem analyzed and the result of this method give the total duration of the project and the associated cost.

This paper aims to give an outline and scope of the study that will be undertaken in this work. Once again, this is too critical that the ability of the project team to identify these paths and formulate
policies and procedures to measure and monitor the critical paths if there are large amount of data. Thus, the focus of this study is to determine the total duration and the associated cost using Critical Path Method.

## 2. MODEL DESCRIPTION

Here, it is shown C Programming Language to compute the total duration and the total cost of the project. The procedure consists of many variables to compute, is the study of the focal study. The Variables are

1) Normal Cost: It is the lowest cost of completing an activity in minimum time employing normal means that is not using overtime or special resources. The variable is ncost.
2) Normal Time: It is minimum time required to achieve the actual cost. The variable is ntime.
3) Crash Cost: It is a least cost of completing an activity by employing all possible means like overtime, additional machinery and proper materials. The variable is ccost.
4) Crash Time: It is an absolute minimum time associated with the crash cost. The variable is ctime
5) Critical Path: It is the sequence of project network terminal elements with the longest overall duration, determining the shortest time to complete the project.
6) The earliest start time (estime): It is the time when an activity can start without affecting the total project time. If the activity has no predecessor, its estime[i] $=0$, otherwise its earliest start time is calculated as estime $[\mathrm{i}]=$ maximum value of earliest starting time of predecessor activities + ntime[i]
7) The earliest finish time (eftime): It is the earliest possible time at which an activity can finish without affecting the total project time. eftime[i] =estime[i]+ntime[i].
8) The latest start time (lstime): It is the latest possible time by which an activity must start without affecting the total of the project. lstime[i]=lftime[i]-ntime[i].
9) The latest finish time (lftime): It is the latest time by which an activity must get completed without delaying the project completion.
lftime[i] =minimum value of latest finish time of successor activitiesntime[i].
10) Slack: the slack time for an activity delivers to the durability of time that can be endured without incurring a delay in the scheduled projection time of completion. The slack time per activity needs to be measured primarily to recognize the critical path, by considering either the begin time of finish time. Hence, for each of the activities in the project network, the slack time can be calculated as
slack $=$ lftime[i]-eftime[i] i.e., $\mathrm{i}=0$ to 7
Consider an example, the slack [1] is
slack[1]=lftime[1]-eftime[1] i.e., slack[1]=8-8, slack[1]=0
11) Total project duration (tdur): Project completion duration computed using critical path method (CPM).
tdur=0;
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{
if(slack[i]==0)
\{
tdur=tdur+ntime[i];
\}\}
12) Indirect cost (incost): Project overhead/indirect cost. This is a fixed monetary value expended each duration unit the project elapses.

## 3. PROCEDURE

The procedure for abbreviating and finding the project duration can be short out in the following steps:

Step 1: Declaring variables for normal time, crash time, crash cost, normal cost, earliest start time, earliest finish time, latest start time, latest finish time and slack so on.

Step 2: Imparting values to ntime,ctime, ncost and ccost according to their source path to destination path.

Step 3: Compute the value for earliest start time, earliest finish time, latest start time, latest finish time and also slack for all activities.

Step 4: Perform CPM calculations and identity the critical path, using slack value which is equal to zero and find the total duration of the project.

Step 5: Compute the Direct cost value by summing all the activities normal cost values and the resultant value is obtained.

Step 6: Getting the value for Indirect cost, the Total cost of the project is calculated by adding the direct cost value with the value which is the indirect cost multiplied with total duration of the project.

## 4. APPLICATION OF THE MODEL ON HYPOTHETICAL PROJECT

Giving input values for activities source, destination, normal time, crash time, normal cost and crash cost of example project by user. These values assigned to the variables of source[i], destination[i], ntime[i] and ctime[i] respectively as well as all the activities ncost[i],ccost[i] values through the C program.

| Source | Destination | Normal <br> Time <br> (Days) | Crash <br> Time <br> (Days) | Normal <br> Cost(\$) | Crash <br> Cost(\$) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | 10 | 7 | 20000 | 30000 |
| 1 | 2 | 8 | 6 | 15000 | 20000 |
| 2 | 4 | 5 | 4 | 8000 | 14000 |
| 2 | 3 | 6 | 4 | 11000 | 15000 |
| 3 | 4 | 0 | 0 | 0 | 0 |
| 2 | 5 | 8 | 5 | 9000 | 15000 |
| 5 | 6 | 5 | 4 | 5000 | 8000 |
| 4 | 6 | 12 | 8 | 3000 | 4000 |

Table 1. Project Information table

Based on the formulae, lstime, lftime, estime and eftime to be calculated as well as the resultant values are assigned. Critical path is identified based on the slack value of each activity. If the activities slack value is zero then the critical path exists in that activity. And the corresponding project completion duration is computed. Under the normal circumstance the cost of this project is obtained from the program by retrieving from the variable tcost which is calculated by summing all the normal cost and the indirect cost.

## 5. PROGRAM

\#include<stdio.h> \#include<conio.h> \#include<math.h> voidmain()
\{ int estime[20],eftime[20],lstime[20],lft,spath[20],dpath[20];
float slope[20],mrt[20],sum,tcost;
intb,a,d,c,g,new3[20],min2[20],slack[20],add[20],tdur;
int incost,f,count,mslope[20];
int
source[20], des[20],ntime[20],ctime[20],np[20],ns[20],ncost[20],cco st[20];
inti,j,k,m,p,x,y,temp,e,z,h,es[20],min[20],new2[20],s,u,q,temp1; int newl[20],max[20],lftime[20],w,l,t,n,de,dd,dc[20];
clrscr();
printf("\nEnter total number of source:");
scanf("\%d",\&n);
printf("\nEnter the source values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n}+1 ; \mathrm{i}++$ )
\{ scanf("\%d",\&source[i]); \}
printf("\nEnter destination values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ printf("\n\%d-->:",source[i]);
scanf("\%d",\&des[i]); \}
printf("\nEnter normal time values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{printf("\n\%d-->\%d:",source[i],des[i]);
scanf("\%d",\&ntime[i]);\}
printf("\nEnter crash time values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{printf("\n\%d-->\%d:",source[i],des[i]);
scanf("\%d",\&ctime[i]); \}
printf("\nEnter normal cost values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{printf("\n\%d-->\%d:",source[i],des[i]);
$\operatorname{scanf}(" \% \mathrm{~d} ", \& n \operatorname{cost}[\mathrm{i}]) ;\}$
printf("\nEnter crash cost values one by one:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ printf("\n\%d-->\%d:",source[i],des[i]);
$\operatorname{scanf}(" \% \mathrm{~d} ", \& \operatorname{cost}[\mathrm{i}]) ;\}$
printf("\nEnter predecessor( front node) of each source:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n}+1 ; \mathrm{i}++$ )
\{ printf("\n\%d:",source[i]);
scanf("\%d",\&np[i]); \}
printf("\nEnter successor(next node) of each source:");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ printf("\n\%d:",des[i]);
scanf("\%d",\&ns[i]); \}
for(i=0;i<n;i++)
$\{$ if(np[i]==0)
\{ estime[i]=0;\}
else if(np[i]==1)
$\{\operatorname{for}(\mathrm{j}=0 ; \mathrm{j}<\mathrm{n} ; \mathrm{j}++)$
\{if(source[i]==des[j])
\{ estime[i]=estime[j]+ntime[j]; \}\}\}
else
\{if(np[i]>1)
\{ $\mathrm{k}=0$;
temp=source[i];
for $(\mathrm{j}=0 ; \mathrm{j}<\mathrm{n} ; \mathrm{j}++$ )
\{if(temp==des[j])
\{newl[k]=source[j];
k++; \}\}
$\mathrm{x}=0$;
for $(\mathrm{w}=0 ; \mathrm{w}<\mathrm{n} ; \mathrm{w}++$ )
$\{$ for $(p=0 ; p<k ; p++)$
$\{$ if((source $[\mathrm{w}]==$ newl $[\mathrm{p}]) \& \&(\operatorname{des}[\mathrm{w}]==$ temp $))$
$\{\max [\mathrm{x}]=$ estime $[\mathrm{w}]+$ ntime $[\mathrm{w}] ; \mathrm{x}++;\}\}\}$
for ( $\mathrm{t}=0 ; \mathrm{t}<\mathrm{n} ; \mathrm{t}++$ )
\{if(source[t]==temp)
estime $[\mathrm{t}]=$ maximum $(\max , \mathrm{x}) ;\}\}\}\}$
$\mathrm{y}=0$;
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ eftime[i]=estime[i]+ntime[i];
if(i==(n-1))
\{de=des[i];
printf("de=\%d",de);
for $(\mathrm{d}=0 ; \mathrm{d}<\mathrm{n} ; \mathrm{d}++$ )
\{if(de==des[d])
\{dd=eftime[d];
dc[y]=dd;
printf(" $\operatorname{ndc}[\% \mathrm{~d}]=\% \mathrm{~d}$ ",y,dc[y]);
y++;\}\}
lft=maximum(dc,y); \}\}
for $(\mathrm{i}=\mathrm{n}-1 ; \mathrm{i}>=0 ; \mathrm{i}--)$
\{ if(ns $[\mathrm{i}]==0)$
\{lftime[i]=lft; \}
else if( $\mathrm{ns}[\mathrm{i}]==1$ )
\{ $\operatorname{for}(\mathrm{j}=\mathrm{n} ; \mathrm{j}>=0 ; \mathrm{j}--)$
\{if(des[i]==source[j])
\{lftime[i]=lftime[j]-ntime[j]; \}\}\}
else
\{if(ns[i]>1)
\{d=0; templ=des[i];
for ( $\mathrm{m}=\mathrm{n} ; \mathrm{m}>=0 ; \mathrm{m}--$ )
\{ if(des[i]==source[m])
\{ new2[d]=des[m];d++;\}\}
$\mathrm{s}=0$;
for $(\mathrm{p}=\mathrm{n}-1 ; \mathrm{p}>=0 ; \mathrm{p}--)$
$\{\operatorname{for}(\mathrm{b}=0 ; \mathrm{b}<\mathrm{d} ; \mathrm{b}++$ )
\{if(source[p]==new2[b])
$\{\min [\mathrm{s}]=\mathrm{lftime}[\mathrm{p}]-\mathrm{ntime}[\mathrm{p}] ; \mathrm{s}++;\}\}\}$
$\mathrm{x}=0$;
for (z=n-1;z>=0;z--)
\{if(source[z]==temp1)
\{min2[x]=lftime[z]-ntime[z]; $\mathrm{x}++;$ \}\}
for $(\mathrm{t}=\mathrm{n}-1 ; \mathrm{t}>=0 ; \mathrm{t}--)$
$\{\operatorname{if}(\operatorname{des}[t]==t e m p 1)$
\{lftime[t]=minimum(min2,x); $\}\}\}\}\}$
// latest starting
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{lstime[i]=lftime[i]-ntime[i];\}
// slack
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{slack[i]=lftime[i]-eftime[i];\}
printf("\nsource des ntime ctime ncost ccost np ns estime eftime lftime lstime slack");
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{printf("\n\%4d\%4d\%4d\%4d\%7d\%7d\%4d\%4d\%4d\%4d\%4d
$\% 4 d \% 4 d^{\prime}$,source[i],des[i],ntime[i],ctime[i],ncost[i],ccost
[i],np[i],ns[i],estime[i],eftime[i],lftime[i],lstime[i],slack[i]); \}
//criticalpath
printf("\n\n\n\ncritical path:");
$\mathrm{f}=0 ; \mathrm{t}=0$;
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{if(slack[i]==0)
\{ spath $[\mathrm{t}]=$ source $[\mathrm{i}]$;
dpath $[\mathrm{t}]=\operatorname{des}[\mathrm{i}]$;
f++;t++;
printf(" \%d-->\%d",source[i],des[i]);\}\}
// total duration
tdur=0;
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ if(slack $[\mathrm{i}]==0)$
\{tdur=tdur+ntime[i];\}\}
printf("\n\nTotal duration:\%d",tdur);
printf("\n\nEnter indirect cost:");
scanf("\%d",\&incost);
// total normal cost
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{n} ; \mathrm{i}++$ )
\{ sum=sum+ncost[i];\}
printf("\n\nTotal normal cost:\%6.0f",sum);
// calculate total cost
tcost=sum+(tdur*incost);
printf("\n\nTotal cost = \%6.0f",tcost);
getch();
\}
int maximum(int m[],int v)
\{ intbig,i;
big=m[0];
for $(\mathrm{i}=0 ; \mathrm{i}<\mathrm{V} ; \mathrm{i}++$ )
\{if(big<m[i])
big=m[i];\}
return(big);
\}
int minimum(intm[],intv)
\{intsmall,i;
small $=\mathrm{m}[0]$;
for(i=0;i<v;i++)
\{if(small>m[i])
small $=\mathrm{m}[\mathrm{i}] ;$ \}
return(small);
\}
6. OUTPUT

| Source des | ntim <br> e | cti <br> me | ncost | ccost | np | ns <br> estim <br> e | efti <br> me | lftim <br> e | sti <br> me | slack |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 4 | 10 | 7 | 20000 | 30000 | 0 | 1 | 0 | 10 | 14 | 4 | 4 |
| 1 | 2 | 8 | 6 | 15000 | 20000 | 0 | 3 | 0 | 8 | 8 | 0 | 0 |
| 2 | 4 | 5 | 4 | 8000 | 14000 | 1 | 1 | 8 | 13 | 14 | 9 | 1 |
| 2 | 3 | 6 | 4 | 11000 | 15000 | 1 | 1 | 8 | 14 | 14 | 8 | 0 |
| 3 | 4 | 0 | 0 | 0 | 0 | 1 | 1 | 14 | 14 | 14 | 14 | 0 |
| 2 | 5 | 8 | 5 | 9000 | 150000 | 1 | 1 | 8 | 16 | 21 | 13 | 5 |
| 5 | 6 | 5 | 4 | 5000 | 8000 | 1 | 0 | 16 | 21 | 26 | 21 | 5 |
| 4 | 6 | 12 | 8 | 3000 | 4000 | 3 | 0 | 14 | 26 | 26 | 14 | 0 |

Criticalpath: 1-->2 $2-->3 \quad 3-->4 \quad 4-->6$
Total duration: 26
Enter indirect cost: 300
Total normal cost: 71000
Total cost $=78800$

The critical path exists on the path $1 \rightarrow 2$, its normal time is 8 , the next critical path $2 \rightarrow 3$, its normal time is 6 , the next critical path $3 \rightarrow 4$, its normal time is 0 and the other critical path $4 \rightarrow 6$, its normal time is 12 , these normal time will be summed to find the total duration of the project (26). The program analyses the data and given the solution that the total duration is 26 days.

The implementation of the program showed more efficient and reliable results and generated a remarkable utilization and saving along with an increase in robustness.

## 7.ANALYSIS AND RESULTS

Exploring the method of finding the total duration of the project and their cost is the major criteria of the study. Using C programming language and run on an example data set, a program was created. The output of the model indicates that the total duration of the project is 26 days and the cost is Rs. 78800 when the indirect cost is 300 .

## 8. CONCLUSION

This study shows ,a C program that is created to equip the total duration and the cost. It is resulted, the project managers schemes of inputs and its consequences of output. Its reliable result of feeding and earning, the project manager wishes to moderate the value of indirect cost, the method will be resulted as the total duration and cost of the project. It proposes a condition; a large number of activities of manual approach are very difficult process, complex and time consuming.

## 9. REFERENCES

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