MHD vicous viscoelastic fluid through magnetic field



Mathematics

KEYWORDS:

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ABSTRACT

Synthesis of coumarins by the reaction of phenols with ethyl acetoacetate (Pechmann reaction) in presence of different Heteropoly acids (HPA) modified Bentonite (STA-Ben, PTA-Ben) as catalysts with high yields, under $mild\ reaction\ conditions\ in\ short\ reaction\ time\ have\ been\ reported.\ HPA-Ben\ have\ been\ synthesized\ and\ characterized\ by\ various\ analytical$ techniques. It has been found to be an efficient and reusable catalyst for the synthesis of coumarin derivatives in excellent yields. Other solid acid catalysts were tested for comparison reasons. The reaction conditions (time and amount of catalyst) have been optimized using various catalysts.

Introduction

The interest in MHD fluid flows stems from the fact the liquid metals that occur in nature and industry are electrically conducting. Naturally, studies of these systems are mathematically interesting and physically useful dynamical study of such flow problems is quite complicated, However, there problems are usually investigated under various simplifying assumptions. First order reactant in MHD turbulence before the final period of decay for the case of multipoint and multi-time has been given by M.A. Islam and Sarkar⁸. Alyub Khan and Bhatia investigated stability of two superposed viscoelastic fluids in a horizontal magnetic field. Gupta and Bhatia² have studied the stability of the plane interface between two viscous superposed partially lonized plasma of uniform. Insities in a uniform two dimensional horizontal magnetic field Srivastava and Khare' have investigated the Rayleigh - Taylor instability of two viscous superposed conducting fluids on a vertical magnetic field. Daval Osorozco⁷ has studied the Reyleigh Taylor instability of a two fluid layer under a general rotation field and horizontal magnetic field. Elgowainy and Ashgriz⁴ have investigated the Rayleigh-Talor instability of viscous fluid layers more recently. Bhatia and Sharma have studied the instability of the plane interface between two viscous fluids through porous medium under a uniform vertical magnetic field. P. Kumar and N.P. Singh¹⁴ have investigated MHD Hele-shaw flow of an elastico viscous fluid through porous medium B. Yadav and Ray studied unsteady flow of n-immiscible visco-elastic fluids through a porous medium between two parallel plates in the presence of a transverse magnetic field.

M.F. El Sayeed9 has recently investigated the electro-hydrodynamics instability of two superpose viscous streaming fluid through porous media. G.D. Gupta and Joha investigated MHD tree dimensional flow past a porous plate. N.D. Anglo and Song 11 & 12 have studied the Kelvin-Helmholtz instability problem in superposed dusty plasma.

Frguven has considered the dynamical Reissner-Sagocci problem for a radially non-homogeneous material. Pal and Kumar 15 have shown the effect of inhomogeneity on torsional impulsive motion over a circular region in a transversely isotropic elastic half-space. In another paper, Pal and Kumar 16 have considered the generation and propagation of SH-waves due to stress discontinuity in a linear viscoelastic layered medium. Recently existence and propagation of torsional surface waves on viscoelastic medium have been discussed by Dey et al¹⁷.

In this paper we have investigated MHD viscous viscelastic fluid through magnetic field.

NOMENCLATURE

B₀=Magnetic field component along y-axisPC=Specific heat of fluid at constant pressure

g = Acceleration due to gravity

k=Thermal conductivity of the fluid='KPermeability of the porous

medium.

K=Permeability parameter

L=Half-wave length of the periodic suction velocity

M=Hartmann number='ppressure

P=Prandtl number

R=Reynolds number='TTemperature of the fluid='wTTemperature of the plate=\infty' TTemperature of the fluid far away from the plate="",,wvu

Velocity components in ",,zyxdirections u,v,w=Dimensionless velocity components

U=Free stream velocitysystemcoordinatezyx=",,,

y,z=Dimensionless coordinatesp=Density of the fluid=vKinematic viscosity=μviscosity=αsuction parameter

Formulation of Problem

Consider three dimensional flow of viscous-incompressible fluid through a highly porous medium which is bounded by a vertical infinite porous plate.

Continuity equation:-

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$$
 (1)

Momentum Equation

$$u^{'}\frac{\partial u^{'}}{\partial x^{'}} + v^{'}\frac{\partial u^{'}}{\partial y^{'}} + w\frac{\partial u^{'}}{\partial z^{'}} = -\frac{1}{\rho}\frac{\partial p^{'}}{\partial x^{'}} + v\left(\frac{\partial^{2}u^{'}}{\partial x^{'2}} + \frac{\partial^{2}v^{'}}{\partial y^{'2}} + \frac{\partial^{2}z^{'}}{\partial z^{'2}}\right) - \frac{\sigma B_{0}^{2}u^{'}}{\rho}$$

$$(2)$$

$$u'\frac{\partial v'}{\partial x'} + v'\frac{\partial v'}{\partial y'} + w'\frac{\partial v'}{\partial z'} = -\frac{1}{\rho}\frac{\partial p'}{\partial y'} + v\left(\frac{\partial^2 v'}{\partial x'^2} + \frac{\partial^2 v'}{\partial y'^2} + \frac{\partial v'}{\partial z'^2}\right) - \frac{\sigma B_0^2 v'}{\rho}$$
(3)

$$u'\frac{\partial w'}{\partial x'} + v'\frac{\partial w'}{\partial y'} + w'\frac{\partial w'}{\partial z'} = -\frac{1}{\rho}\frac{\partial p'}{\partial z'} + v\left(\frac{\partial^2 w'}{\partial x'^2} + \frac{\partial^2 w'}{\partial y'^2} + \frac{\partial w'}{\partial z'^2}\right) - \frac{\sigma B_0^2 w'}{\rho}$$

$$\tag{4}$$

$$\rho Cp \left(u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} + w \frac{\partial T}{\partial z} \right) = k \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} + \frac{\partial^2 T}{\partial z^2} \right)$$

(5)

We now introduce the following non-dimensional variables:

$$y = \frac{y'}{d}, z = \frac{z'}{d}, u = \frac{u'}{v}, v = \frac{v'}{v}, p = \frac{p'}{pv^2}$$

$$\theta = \left(\frac{T' - T_o}{T_1 - T_o}\right)$$

Prandtl Number (P): $p = \frac{\mu C_p}{k}$

Reynold's Number (R) :
$$R = \frac{UL}{V}$$

Harmann Number (M) : $M = \frac{\sigma B_o^2 v L}{U \mu}$

Permeability Parameter (k): $K = \frac{K'U^2}{v^2}$

Suction Parameter (α) : $\alpha = \frac{V}{U}$

Kinematic coefficient viscosity (v): $v = \frac{\mu}{\rho}$

With the help of the above non-dimensional variables eq (1) to (5) become:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \tag{6}$$

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} + w\frac{\partial u}{\partial z} = -\frac{\partial p}{\partial x} + \frac{1}{R} \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) - Mu \tag{7}$$

$$u\frac{\partial v}{\partial x} + v\frac{\partial v}{\partial y} + w\frac{\partial v}{\partial z} = -\frac{\partial p}{\partial y} + \frac{1}{R} \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right) - Mv \tag{8}$$

$$u\frac{\partial w}{\partial x} + v\frac{\partial w}{\partial y} + w\frac{\partial w}{\partial z} = -\frac{\partial p}{\partial z} + \frac{1}{R} \left(\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) - Mw \tag{9}$$

$$u\frac{\partial\theta}{\partial x} + v\frac{\partial\theta}{\partial y} + w\frac{\partial\theta}{\partial z} = \frac{1}{PR} \left(\frac{\partial^2\theta}{\partial x^2} + \frac{\partial^2\theta}{\partial y^2} + \frac{\partial^2\theta}{\partial z^2} \right)$$
(10)

Solution of the Problem and Results

In order to solve these differential equations, we assume that.

Case I

$$U(X, Y, Z) = U_{o}(X) + \varepsilon U_{1}(X, Y, Z), \tag{11}$$

$$V(X, Y, Z) = V_o(X) + \varepsilon V_1(X, Y, Z), \tag{12}$$

$$W(X, Y, Z) = W_{\circ}(X) + \varepsilon W_{1}(X, Y, Z), \tag{13}$$

$$p(x, y, z) = p_{o}(x) + \varepsilon p_{1}(x, y, z), \tag{14}$$

and

$$\theta(X, Y, Z) = \theta_0(X) + \varepsilon \theta_1(X, Y, Z), \tag{15}$$

partially diff. eq. (11) w. r. t. x

$$\frac{\partial u}{\partial x} = \frac{\partial u_o}{\partial x} + \varepsilon \frac{\partial u_1}{\partial x} \tag{16}$$

again p. diff. w. r. t. x

$$\frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u_o}{\partial x^2} + \varepsilon \frac{\partial^2 u_1}{\partial x^2}$$
 (17)

p. diff. eq. (11) w. r. t. y

$$\frac{\partial u}{\partial y} = \varepsilon \frac{\partial u_1}{\partial y} \tag{18}$$

again diff. w. r. t. to y

$$\frac{\partial^2 u}{\partial y^2} = \varepsilon \frac{\partial^2 u_1}{\partial y^2} \tag{19}$$

p. diff. eq. (11) w. r. t. to z

$$\frac{\partial \mathbf{u}}{\partial \mathbf{z}} = \varepsilon \frac{\partial \mathbf{u}_1}{\partial \mathbf{z}} \tag{20}$$

Again diff. w. r. t. z

$$\frac{\partial^2 \mathbf{u}}{\partial \mathbf{z}^2} = \varepsilon \frac{\partial^2 \mathbf{u}_1}{\partial \mathbf{z}^2} \tag{21}$$

p. diff. eq (12) w. r. t. x

$$\frac{\partial V}{\partial x} = \frac{\partial V_o}{\partial x} + \varepsilon \frac{\partial V_1}{\partial x} \tag{22}$$

Again Diff. w. r. t. x

$$V_o \frac{\partial \theta_o}{\partial y} = \frac{1}{PR} \frac{\partial^2 \theta_o}{\partial y^2}$$
 (23)

p. diff. Eq (12) w. r. to y

$$\frac{\partial V}{\partial V} = \varepsilon \frac{\partial V_1}{\partial V} \tag{24}$$

Again diff. w. r. t. y

$$\frac{\partial^2 \mathbf{V}}{\partial \mathbf{V}^2} = \varepsilon \frac{\partial^2 \mathbf{V}_1}{\partial \mathbf{V}^2} \tag{25}$$

diff.Eq.(12) w.r.t.z

$$\frac{\partial \mathbf{v}}{\partial \mathbf{z}} = \varepsilon \frac{\partial \mathbf{v}_1}{\partial \mathbf{z}} \tag{26}$$

Again diff. w. r. t. z

$$\frac{\partial^2 \mathbf{V}}{\partial \mathbf{z}^2} = \varepsilon \frac{\partial^2 \mathbf{V_1}}{\partial \mathbf{z}^2} \tag{27}$$

p. diff. eq. (13) w. r. t. x

$$\frac{\partial W}{\partial x} = \frac{\partial W}{\partial x} + \varepsilon \frac{\partial W}{\partial x}$$
 (28)

Again diff. w. r. t. x

$$\frac{\partial^2 \mathbf{W}}{\partial \mathbf{x}^2} = \frac{\partial^2 \mathbf{W}_o}{\partial \mathbf{x}^2} + \varepsilon \frac{\partial^2 \mathbf{W}_1}{\partial \mathbf{x}^2} \tag{29}$$

p. diff. eq. (13) w. r. t. y

$$\frac{\partial W}{\partial y} = \varepsilon \frac{\partial W_1}{\partial y} \tag{30}$$

Again diff.

$$\frac{\partial^2 W}{\partial y^2} = \varepsilon \frac{\partial^2 W_1}{\partial y^2} \tag{31}$$

p. diff. eq. (13) w. r. t. z

$$\frac{\partial^2 W}{\partial z^2} = \varepsilon \frac{\partial^2 W_1}{\partial z^2} \tag{33}$$

Again diff.

$$\frac{\partial p}{\partial x} = \frac{\partial p_o}{\partial x} + \varepsilon \frac{\partial p_1}{\partial x}$$
 (34)

p. diff. eq. (14) w. r. t. x

$$\frac{\partial p}{\partial y} = \frac{\partial p_o}{\partial y} + \varepsilon \frac{\partial p_1}{\partial y}$$
 (35)

p. diff. eq. (14) w. r. t. z

$$\frac{\partial p}{\partial z} = \frac{\partial p_o}{\partial z} + \varepsilon \frac{\partial p_1}{\partial z}$$
 (36)

put the values of $\frac{\partial u}{\partial x}, \frac{\partial v}{\partial y}, \frac{\partial w}{\partial z}$ in eq (6) from eq. no.s (16),(24) and

$$\frac{\partial u_o}{\partial x} + \varepsilon \frac{\partial u_1}{\partial x} + \varepsilon \frac{\partial v_1}{\partial y} + \varepsilon \frac{\partial w_1}{\partial z} = 0$$
 (37)

equating the terms of free from ϵ

$$\frac{\partial u_o}{\partial x} = 0 \quad \text{i. e. } u_0' = 0 \tag{38}$$

Put the values of $\frac{\partial u}{\partial x}$, $\frac{\partial u}{\partial y}$, $\frac{\partial u}{\partial z}$, $\frac{\partial u}{\partial x^2}$, $\frac{\partial^2 u}{\partial x^2}$, $\frac{\partial^2 u}{\partial z^2}$ and $\frac{\partial p}{\partial x}$, u, v, w, in eq (7) from eq no.

$$\begin{split} & \left(u_{o} + \varepsilon u_{1} \left(\frac{\partial u_{o}}{\partial x} + \varepsilon \frac{\partial u_{1}}{\partial x}\right) + \left(v_{o} + \varepsilon v_{1}\right) \left(\varepsilon \frac{\partial u_{1}}{\partial y}\right) + \left(w_{o} + \varepsilon w_{1}\right) \left(\varepsilon \frac{\partial u_{1}}{\partial z}\right) \\ & = -\frac{\partial p_{o}}{\partial x} - \varepsilon \frac{\partial p_{1}}{\partial x} + \frac{1}{R} \left(\frac{\partial^{2} u_{o}}{\partial x^{2}} + \varepsilon \frac{\partial^{2} u_{1}}{\partial x^{2}} + \varepsilon \frac{\partial^{2} u_{1}}{\partial y^{2}} + \varepsilon \frac{\partial^{2} u_{1}}{\partial z^{2}}\right) - M(u_{0} + \varepsilon u_{1}) \end{split}$$
(39)

equating the terms free from ϵ

$$u_{o} \frac{\partial u_{o}}{\partial x} = -\frac{\partial p_{o}}{\partial x} + \frac{1}{R} \left(\frac{\partial^{2} u_{o}}{\partial x^{2}} \right) - Mu_{o}$$

$$u_{o}u_{o}R = -p_{o}R + u_{o}^{"} MRu_{o}$$

$$-u_{o}^{"} + u_{o}Ru_{o} + Rp_{o} + MRu_{o} = 0$$

$$u_{o}^{"} - u_{o}Ru_{o} - Rp_{o} - MRu_{o} = 0$$
(40)

Put the values of $\frac{\partial v}{\partial x}, \frac{\partial v}{\partial y}, \frac{\partial v}{\partial z}, \frac{\partial^2 v}{\partial x^2}, \frac{\partial^2 v}{\partial y^2}, \frac{\partial^2 v}{\partial z^2}$ and $\frac{\partial p}{\partial x}, u, v, w$ in eq (8) from eq no.-

$$\left(\textit{U}_{o}+\textit{\varepsilon}\,\textit{U}_{1}\right)\!\!\left(\!\frac{\partial\textit{V}_{o}}{\partial\textit{x}}+\textit{\varepsilon}\frac{\partial\textit{V}_{1}}{\partial\textit{x}}\!\right)\!+\!\left(\!\textit{V}_{o}+\textit{\varepsilon}\,\textit{V}_{1}\!\right)\!\!\left(\!\textit{\varepsilon}\frac{\partial\textit{V}_{1}}{\partial\textit{y}}\!\right)\!+\!\left(\!\textit{W}_{o}+\textit{\varepsilon}\,\textit{W}_{1}\!\right)\!\!\left(\!\textit{\varepsilon}\frac{\partial\textit{V}_{1}}{\partial\textit{z}}\!\right)$$

$$= -\frac{\partial p_o}{\partial x} + \frac{1}{R} \left[\frac{\partial^2 V_o}{\partial x^2} + \varepsilon \frac{\partial^2 V_1}{\partial x^2} + \varepsilon \frac{\partial^2 V_1}{\partial y^2} + \varepsilon \frac{\partial^2 V_1}{\partial z^2} \right] - M(V_0 + \varepsilon V_1)$$
(41)

equating the terms free from eq. (41)

$$u_{o} \frac{\partial v_{o}}{\partial x} = \frac{1}{R} \left(\frac{\partial^{2} v_{o}}{\partial x^{2}} \right) - Mu_{o}$$

$$u_{o} v_{o}' R = v_{o}'' - MRv_{o}$$

$$- v_{o}' + u_{o} R v_{o}' + MRv_{o} = 0$$

$$v_{o}'' - u_{o} R v_{o}' - MRv_{o} = 0$$
(42)

Put the values of $\frac{\partial w}{\partial x}$, $\frac{\partial w}{\partial y}$, $\frac{\partial w}{\partial z}$, $\frac{\partial^2 w}{\partial z^2}$, $\frac{\partial^2 w}{\partial y^2}$, $\frac{\partial^2 w}{\partial y^2}$, $\frac{\partial^2 w}{\partial z^2}$ and u,v,w in eq (9) from eq no.

$$\left(u_{o} + \varepsilon u_{1} \left(\frac{\partial w_{o}}{\partial x} + \varepsilon \frac{\partial w_{1}}{\partial x}\right) + \left(v_{o} + \phi v_{1} \left(\varepsilon \frac{\partial w_{1}}{\partial y}\right) + \left(w_{o} + \varepsilon w_{1}\right) \left(\varepsilon \frac{\partial w_{1}}{\partial z}\right) \right) \\
= -\frac{\partial p_{1}}{\partial x} + \frac{1}{R} \left(\frac{\partial^{2} w_{o}}{\partial x^{2}} + \varepsilon \frac{\partial^{2} w_{1}}{\partial x^{2}} + \varepsilon \frac{\partial^{2} w_{1}}{\partial y^{2}} + \varepsilon \frac{\partial^{2} w_{1}}{\partial z^{2}}\right) - M(w_{0} + \varepsilon w_{1}) \tag{43}$$

equating the terms free from ϵ from eq. (43)

$$u_o \frac{\partial w_o}{\partial x} = \frac{1}{R} \left(\frac{\partial^2 w_o}{\partial x^2} \right) - M w_o$$

$$- w_o'' + u_o R w_o' + M R w_o = 0$$

$$w_o'' - u_o R w_o' - M R w_o = 0$$
(44)

$$u\frac{\partial \theta}{\partial x} + v\frac{\partial \theta}{\partial y} + w\frac{\partial \theta}{\partial z} = \frac{1}{PR} \left(\frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial y^2} + \frac{\partial^2 \theta}{\partial z^2} \right)$$

partially diff. eq (15) w. r. t. x

$$\frac{\partial \theta}{\partial \mathbf{x}} = \frac{\partial \theta_{o}}{\partial \mathbf{x}} + \varepsilon \frac{\partial \theta_{1}}{\partial \mathbf{x}} \tag{45}$$

Again diff. eq w.r.t.x

$$\frac{\partial^2 \theta}{\partial \mathbf{x}^2} = \frac{\partial^2 \theta_o}{\partial \mathbf{x}^2} + \varepsilon \frac{\partial^2 \theta_1}{\partial \mathbf{x}^2} \tag{46}$$

Partially diff. eq (15) w. r. t. v

$$\frac{\partial \theta}{\partial y} = \varepsilon \frac{\partial \theta_1}{\partial y} \tag{47}$$

Again diff. eq w.r.t.y

$$\frac{\partial^2 \theta}{\partial y^2} = \varepsilon \frac{\partial^2 \theta_1}{\partial y^2} \tag{48}$$

Partially diff. eq (15) w. r. t. z

$$\frac{\partial \theta}{\partial \mathbf{z}} = \varepsilon \frac{\partial \theta_1}{\partial \mathbf{z}} \tag{49}$$

Again diff. eq w.r.t. z

$$\frac{\partial^2 \theta}{\partial \mathbf{z}^2} = \varepsilon \frac{\partial^2 \theta_1}{\partial \mathbf{z}^2} \tag{50}$$

Put the values of $\frac{\partial \theta}{\partial x}$, $\frac{\partial \theta}{\partial y}$, $\frac{\partial \theta}{\partial z}$, $\frac{\partial^2 \theta}{\partial z^2}$, $\frac{\partial^2 \theta}{\partial y^2}$, $\frac{\partial^2 \theta}{\partial z^2}$ and u, v, w in eq (9)

$$\begin{aligned}
& \left(U_o + \varepsilon U_1 \left(\frac{\partial \theta_o}{\partial x} + \varepsilon \frac{\partial \theta_1}{\partial x} \right) + \left(V_o + \varepsilon V_1 \left(\varepsilon \frac{\partial \theta_1}{\partial y} \right) + \left(W_o + \varepsilon W_1 \left(\varepsilon \frac{\partial \theta_1}{\partial z} \right) \right) \right. \\
&= - \frac{1}{RP} \left(\frac{\partial^2 \theta_o}{\partial x^2} + \varepsilon \frac{\partial^2 \theta_1}{\partial x^2} + \varepsilon \frac{\partial^2 \theta_1}{\partial y^2} + \varepsilon \frac{\partial^2 \theta_1}{\partial z^2} \right)
\end{aligned} \tag{51}$$

equating the terms free from e from eq. (51)

$$u_o \frac{\partial \theta_o}{\partial \mathbf{y}} = -\frac{1}{RP} \frac{\partial^2 \theta_o}{\partial \mathbf{y}^2}$$
 (52)

$$u_o\theta_o' = -\frac{1}{RP}\theta_o''$$

$$\theta_{\alpha}^{"} + RPu_{\alpha}\theta_{\alpha}^{'} = 0 \tag{53}$$

$$\theta_{a}^{"} + RPu_{a}\theta_{a}^{'} = 0 \tag{53}$$

equating the coefficient of E from eq's (39)

$$u_{o}\frac{\partial u_{1}}{\partial x}+v_{o}\frac{\partial u_{1}}{\partial y}+w_{o}\frac{\partial u_{1}}{\partial z}=-\frac{\partial p}{\partial x}+\frac{1}{R}\left(\frac{\partial^{2}u_{1}}{\partial x^{2}}+\frac{\partial^{2}u_{1}}{\partial y^{2}}+\frac{\partial u_{1}}{\partial z^{2}}\right)-Mu_{1} \tag{54}$$

equating the coefficient of ε from eq. (37)

$$\frac{\partial u_1}{\partial x} + \frac{\partial v_1}{\partial y} + \frac{\partial w_1}{\partial z} = 0$$
 (55)

equating the coffrcient of ϵ from equation (431)

$$u_{0} \frac{\partial v_{1}}{\partial x} + u_{1} \frac{\partial v_{0}}{\partial x} + v_{0} \frac{\partial v_{1}}{\partial y} + w_{0} \frac{\partial v_{1}}{\partial z}$$

$$= -\frac{\partial p}{\partial y} + \frac{1}{R} \left(\frac{\partial^{2} v_{1}}{\partial x^{2}} + \frac{\partial^{2} v_{1}}{\partial y^{2}} + \frac{\partial^{2} v_{1}}{\partial z^{2}} \right) - Mv_{1}$$
(56)

equating the coefficient of ε from equation (46)

$$\boldsymbol{u}_0\,\frac{\partial\boldsymbol{w}_1}{\partial\boldsymbol{x}} + \boldsymbol{u}_1\,\frac{\partial\boldsymbol{w}_0}{\partial\boldsymbol{x}} + \boldsymbol{v}_0\,\frac{\partial\boldsymbol{w}_1}{\partial\boldsymbol{y}} + \boldsymbol{w}_0\,\frac{\partial\boldsymbol{w}_1}{\partial\boldsymbol{z}}$$

$$= -\frac{\partial p_1}{\partial z} + \frac{1}{R} \left(\frac{\partial^2 w_1}{\partial x^2} + \frac{\partial^2 w_1}{\partial y^2} + \frac{\partial^2 w_1}{\partial z^2} \right) - Mw_1$$
 (57)

equating the coefficient of ϵ from equation (51)

$$u_{0} \frac{\partial \theta_{1}}{\partial x} + u_{1} \frac{\partial \theta_{0}}{\partial x} + v_{0} \frac{\partial \theta_{1}}{\partial y} + w_{0} \frac{\partial \theta_{1}}{\partial z} = -\frac{1}{RP} \left(\frac{\partial^{2} \theta_{1}}{\partial x^{2}} + \frac{\partial^{2} \theta_{1}}{\partial y^{2}} + \frac{\partial^{2} \theta_{1}}{\partial z^{2}} \right)$$
(58)

Case I

$$u(x, y, z) = u_o(y) + \varepsilon u_1(x, y, z)$$
(59)

$$V(X, y, z) = V_o(y) + \varepsilon V_1(X, y, z)$$
(60)

$$W(X, Y, Z) = W_o(Y) + \varepsilon W_1(X, Y, Z) \tag{61}$$

$$p(x,y,z) = p_o(y) + \varepsilon p_1(x,y,z)$$
(62)

$$\theta(\mathbf{x}, \mathbf{y}, \mathbf{z}) = \theta_{0}(\mathbf{y}) + \varepsilon \theta_{1}(\mathbf{x}, \mathbf{y}, \mathbf{z}) \tag{63}$$

$$\varepsilon \frac{\partial u}{\partial x} + \varepsilon \frac{\partial v_o}{\partial y} + \varepsilon \frac{\partial v_1}{\partial y} + \varepsilon \frac{\partial w}{\partial z} = 0$$
 (64)

$$(u_{o} + \varepsilon u_{1})\varepsilon \frac{\partial u_{1}}{\partial x} + (v_{o} + \varepsilon v_{1})\left(\frac{\partial u_{o}}{\partial y} + \varepsilon \frac{\partial u_{1}}{\partial y}\right) + (w_{o} + \varepsilon w_{1})\left(\varepsilon \frac{\partial u_{1}}{\partial z}\right)$$

$$= -\left(\varepsilon \frac{\partial p_{1}}{\partial x}\right) + \frac{1}{R}\left(\varepsilon \frac{\partial^{2} u_{1}}{\partial x^{2}} + \frac{\partial^{2} u_{0}}{\partial y^{2}} + \varepsilon \frac{\partial^{2} u_{1}}{\partial y^{2}} + \varepsilon \frac{\partial^{2} w_{1}}{\partial z^{2}}\right) - M(u_{o} + \varepsilon u_{1}) \quad (65)$$

$$\Big(u_0 + \varepsilon u_1\Big)\varepsilon\frac{\partial v_1}{\partial x} + \Big(v_o + \varepsilon v_1\Big)\left(\frac{\partial v_o}{\partial y} + \varepsilon\frac{\partial v_1}{\partial y}\right) + \Big(w_o + \varepsilon w_1\Big)\left(\varepsilon\frac{\partial v_1}{\partial z}\right)$$

$$= -\left(\frac{\partial p_o}{\partial y} + \varepsilon \frac{\partial p_1}{\partial x}\right) + \frac{1}{R} \left(\varepsilon \frac{\partial^2 v_1}{\partial x^2} + \frac{\partial^2 v_0}{\partial y^2} + \varepsilon \frac{\partial^2 v_1}{\partial y^2} + \varepsilon \frac{\partial^2 v_1}{\partial z^2}\right) - M(v_o + \varepsilon v_1)$$
(66)

$$\left(u_{o}+\varepsilon u_{1}\right)\varepsilon\frac{\partial w_{1}}{\partial x}+\left(v_{o}+\varepsilon v_{1}\right)\left(\frac{\partial w_{o}}{\partial y}+\varepsilon\frac{\partial w_{1}}{\partial y}\right)+\left(w_{o}+\varepsilon w_{1}\right)\left(\varepsilon\frac{\partial w_{1}}{\partial z}\right)$$

$$= -\left(\varepsilon \frac{\partial p_1}{\partial x}\right) + \frac{1}{R} \left(\varepsilon \frac{\partial^2 w_1}{\partial x^2} + \frac{\partial^2 w_0}{\partial y^2} + \varepsilon \frac{\partial^2 w_1}{\partial y^2} + \varepsilon \frac{\partial^2 w_1}{\partial z^2}\right) - M(w_o + \varepsilon w_1)$$
 (6)

$$\left(u_{0}+\varepsilon u_{1}\right)\varepsilon\frac{\partial\theta_{1}}{\partial x}+\left(v_{o}+\varepsilon v_{1}\right)\left(\frac{\partial\theta_{o}}{\partial y}+\varepsilon\frac{\partial\theta_{1}}{\partial y}\right)+\left(w_{o}+\varepsilon w_{1}\right)\left(\varepsilon\frac{\partial\theta_{1}}{\partial z}\right)$$

$$= -\frac{1}{PR} \left(\varepsilon \frac{\partial^2 \theta_1}{\partial x^2} + \frac{\partial^2 \theta_0}{\partial y^2} + \varepsilon \frac{\partial \theta_1}{\partial y^2} + \varepsilon \frac{\partial \theta_1}{\partial z^2} \right)$$
 (68)

Equating the terms free from ε

$$\frac{\partial v_o}{\partial y} = 0$$

$$v_o' = 0 \tag{69}$$

$$v_o \frac{\partial u_o}{\partial y} = \frac{1}{R} \frac{\partial^2 u_o}{\partial y^2} - M u_o$$

$$v_o R u'_o - u''_o = -MR u_o$$

 $u''_o - v_o R u'_o + MR u_o = 0$ (70)

$$v_o \, \frac{\partial v_o}{\partial y} = -\frac{\partial p_o}{\partial y} + \frac{1}{R} \frac{\partial^2 v_o}{\partial y^2} - M v_o$$

$$Rv_o v_o' = -Rp_o' + v_o'' - MRv_o$$
 (71)

$$v_o \frac{\partial w_o}{\partial v} = \frac{1}{R} \frac{\partial^2 w_o}{\partial v^2} - M w_o$$

$$v_{o}Rw_{o}^{'} - w_{o}^{"} = -MRw_{o}$$

 $w_{o}^{"} - v_{o}Rw_{o}^{'} + MRw_{o} = 0$ (72)

$$v_o \frac{\partial \theta_o}{\partial v} = \frac{1}{PR} \frac{\partial^2 \theta_o}{\partial v^2}$$

$$PRv_o \theta_o' - \theta_o'' = 0$$

$$\theta'' - PRv_{\bullet}\theta_{\bullet}' = 0 \tag{73}$$

Result

MHD vicous viscoelastic fluid past an infinite, porous plate with constant suction under the action of time dependent plate temperature has been studied, when the plate temperature oscillates about a constant mean in magnitude but not in direction. In the absence of the magnetic field, it is observed that the flow is similar about y-axis where as this phenomenon disappears for non zero values of M.

1. Alyub Khan and P.K. Bhatia, Indian, J. Pure app. Math., 32(1) Jan. (2001) 99-108. [2. A Gupta and P.K. Bhatia. Astrophys space Sci., 181 (1991); 109. [3. A.K. Srivastava and H.C. Khare, Proc. Nat. Acad. 66 (1996); 151. [4. A. Elgowaing and N.Ashgriz; Phys Fluids, (9) (1997); 1635. [5. B. Yadav and T.K. Ray, Proc. Nat. Acad Sci., 81 (1991); 389. [6. G.D. Gupta and Rajesh Johari, Indian, J. Pure appli. Math. 32 (3) (2001) 377-386. [7. L.A. Daval Osorozco, Astrophys space Sci., 243 (1986) 291. [8. M.A. Islam and N.S. Alam Sarkar, Indian, (2001) 1173-1184. [9. M.F. Elsayeed; Conad J. Phys 75 (1997); 499. [10. M.E. Frguven; Int. J. Engng, Sci 26 (1988) 77. [11. N.D. Anglo and B. Song, Plant Space, Sci. 38 (1991) 97. [12. N.D. Anglo and B. Song, IEEE Transector plasma Sci 19 (1991) 42. [13. P.K. Bhatia A. Sharma, Proc. Nat. Acad. Sci. 69 (1999) 171. [14. K. Lwmar and N.P. Singh, Bull. Calcutta, Math. Soc. 83 (1991) 97. [15. P.C. Pal and Islam Kumar; Indian J. Pure apple Math. 24 (2) (1993) 133. [16. P.C. Pal and Islam Kumar; Proc. Indian Acad. Sci. (Math. Sci.) 105(2) (1995) 241. [17. S. Dev. Pal and Islam Kumar; Proc. Indian Acad. Sci. (Math. Sci.) 105(2) (1995) 241. [17. S. Dev. Pal and Islam Kumar; Proc. Indian Acad. Sci. (Math. Sci.) 105(2) (1995) 241. [17. S. Dev. Pal and Islam Kumar; Proc. Pal

Math. Soc. 83(1991) 97.] 15. P.C. Pal and Lalan Kumar; Indian J. Pure apple, Math. 24(2)(1993) 133.] 16. P.C. Pal and Lalan Kumar, Proc. Indian Acad. Sci. (Math Sci) 105(2) (1995) 241.] 17. S. Dey, S. Gupta and A.K. Gupta Int. J. Numer. Anal. Method Geomech., 19 (1996) 209. | 18. Behrouz Raftari, Syed Tauseef Mohyud-Din, Ahmet Yildirim, Science China Physics, Mechanics and Astronomy, February 2011, Volume 54, Issue 2, pp 342-345 | 19. HaoYu Lu, ChunHian Lee, Science in China Series E: Technological Sciences, January 2010, Volume 53, Issue 1, pp 206-212 | 20. M. Kar, S. N. Sahoo, G. C. Dash, Generation Journal of Engineering Physics and Thermophysics, July 2014, Volume 87, Issue 4, p 101 | 21. M. Khan, Madiha Ajmal, C. Fetecau RETRACTED ARTICLE, March 2013, Volume 97, Issue 1, p 133 | 22. D. S. Chauhan, R. Agrawal Journal of Engineering Physics and Thermophysics, January 2012, Volume 85, Issue 1, p 249 | 23. N. Ahmed, J. K. Goswami, D. P. Barua, Indian Journal of Pure and Applied Mathematics, August 2013, Volume 44, Issue 4, pp 443-466 | 24. Rajesh Kumar Gupta and Mahinder Singh, eld, Advances in Applied Science Research, 2012, 3(5):3253-3258 | 25. Mahinder Singh, C. B. Mehta and Sanjeev Gangta, Advances in Applied Science Research, 2012, 3(6):3459-3468