Research Paper

Computer Science



Optimizing Single-Layer Raster Cellular Neural Network simulator using simulated Annealing technique and RK 8(6)

* O.H. Abdelwahed ** M. El-Sayed Wahed

*Assistant Department of Computer Science, Faculty of Computers and Information Suez Canal University, EGYPT

** Associate Professor, Department of Computer Science, Faculty of Computers and Information, Suez Canal University, EGYPT

ABSTRACT

An efficient numerical integration algorithm for single layer Raster Cellular Neural Networks (CNN) simulator is presented in this paper. The simulator is capable of performing CNN simulations for any size of input image, thus a powerful tool for researchers investigating potential applications of CNN. Explicit Runge{Kutta (RK) methods in the form of pairs of orders p (p -1) provide an attractive means for the solution of initial value problems of first-order differential equations. Most existing RK formulas (single methods as well as pairs) use the minimal number of stages required for achieving a prescribed order. In this article we shall study, in terms of efficiency and reliability, RK pairs of orders p (q). This paper reports an efficient algorithm exploiting the latency properties of Cellular Neural Networks along with numerical integration techniques RK4(2), RK4(3), and RK6(4); simulation results and comparisons are also presented.

Keywords : single-layer Cellular neural networks, numerical integration algorithms, RK4(2), 4(3), and RK6(4)

1 Introduction

Explicit RK methods in the form of pairs of embedded methods are currently considered one of the most efficient means for solving the nonstiff initial value problem

$$y_{0} = f(x; y); y(\mathbf{x}_{0}) = y_{0}$$

$$x \in [\mathbf{x}_{0}, y_{0}] f : \mathbb{R} \times \mathbf{R}_{m} \to \mathbf{R}_{m}$$
(1)

An RK method is characterized by the triple A, b, c (where $A \in R^{m}, B^{1}, C \in R^{1}$) and is said to be of algebraic order (or simply order) p, whenever the coefficients in A, b, c satisfy a system of order conditions, which are in one-to-one correspondence with the set of (rooted) trees of orders not exceeding p (see Butcher [11], Hairer, N[°]orsett, and Wanner [12]). RK pairs are characterized by two RK methods of orders p (q), (p > q) with distinct vectors of weights b, ^b, which, however, share the same function evaluations (A, c are the same for both methods).

In practice, the solution of the order conditions for the construction of RK methods or pairs involves the application of a suitable set of simplifying assumptions (see, for example, [11], and for more up-to-date information see [13] and the classification and relevant discussion therein). Although the analysis seems to be complicated (especially for higher-order methods), in most cases (see [15], [14], and [13]) efficient and easily implementable algorithms have been obtained. These algorithms are characterized by a number of free parameters and define certain families of solution of the respective order conditions.

CNN is a hybrid of Cellular Automata and Neural Networks (hence the name Cellular Neural Networks), and it shares the best features of both worlds. Like Neural Networks, its continuous time feature allows real-time signal processing, and like Cellular Automata, its local interconnection feature makes VLSI realization feasible. Its grid-like structure is suitable for the solution of a high order system of first order non-linear differential equations on-line and in real-time.

The basic circuit unit of CNN is called a [2]. It contains linear and nonlinear circuit elements. Any cell, C(i,j), is connected only to its neighbor cells, i.e. adjacent cells interact directly with each other. This intuitive concept is called neighborhood and is denoted as N(i,j). Cells not in the immediate neighborhood have indirect effect because of the propagation effects of the dynamics of the network. Each cell has a state x input U, and output y. The state of each cell is bounded for all time t > U and, after the transient has settled down, a cellular neural network always approaches one of its stable equilibrium points. This last fact is relevant because it implies that the circuit will not oscillate. The dynamics of a CNN has both output feedback (A) and input control (B) mechanisms. The first order nonlinear differential equation defining the dynamics of a cellular neural network cell can be written as follows:

$$C \frac{d \mathbf{x}_{j}(t)}{d} = -\frac{1}{R} \mathbf{x}_{j}(t) + \sum_{c(k,j) \in N(i,j)} A(i, j; k, l) \mathbf{y}_{k}(t) + \sum_{c(k,j) \in N(i,j)} B(i, j; k, l) \mathbf{u}_{k}$$
$$\mathbf{y}_{j}(t) = \frac{1}{2} \left(\mathbf{x}_{j}(t) + 1 | - | \mathbf{x}_{j}(t) - 1 | \right)$$
(2)

where x_i is the state of cell C(i,j), $x_i^{(0)}$ is the initial condition of the cell, C is a linear capacitor, R is a linear resistor, I is an independent current source, A(I,J;k, 1)ykl and B{i,j;k,I)ukl are voltage controlled current Sources for all cells C(k,I) in the neighborhood N(ij) of cell C(ij), and yij represents the output equation.

Notice from the summation operators that each cell is affected by its neighbor cells. A(.) acts on the output of neighboring cells and is referred to as the feedback operator. B(.) in turn affects the input control and is referred to as the control operator. Spe- cific entry values of matrices A(.) and B(.) are application dependent, are space invariant and are called cloning templates. A current bias Z and the cloning templates determine the transient behavior of the cellular nonlinear network.

CNNs have as input a set of analog values and its programmability is done via cloning templates. Thus, programmability is one of the most attractive properties of CNNs, but how to choose the optimal network and how to program it to perform a given task are still topics under investigation. This is the reason why there is a need for behavioral CNN simulator capable of helping investigators design and manipulate cloning templates ("programming"). Existent tools are not meant to deal with a significant number of pixels typical in common image processing applications [5]. The simulator presented here not only satisfies this need, but it also can be used for testing CNN hardware implementations. M. El-Sayed Wahed and O.H. Abdel wahed[1] introduced an efficient numerical integration algorithm for Single-Layer Raster Cellular Neural Networks Simulator. In this paper, we consider the same problem since we optimize their solution by using the optimization technique, simulated annealing.

2 Behavioral Simulation

Recall that equation (1) is space invariant, which means that A(i,j;k,l) = A(i-k,j-1) and B(i,j;k,l) = B(i,k;,j,l) for all i,j,kl.

Therefore, the solution of the system of difference equations can be seen as a convolution process between the image and the CNN processors. The basic approach is to imagine a square subimage area centered at (x,y), with the subimage being the same size of the templates involved in the simulation. The center of this subimage is then moved from pixel to pixel starting, say, at the top left comer and applying the A and B templates at each location (x,y) to solve the differential equation. This procedure is repeated for each time step, for all the pixels. An instance of this image scanning-processing is referred to as an "iteration". The processing stops when it is found that the states of all CNN processors have converged to steady-state values[2] and the outputs of its neighbor cells are saturated, e.g. they have a +1 value.

This whole simulating approach is referred to as raster simulation. A simplified algorithm is presented below for this approach. The part where the integration is involved (i.e. calculation of the next state) is explained in the Numerical Integration Methods section.

In the following two subsections we will discuss simulated annealing algorithm and the mathematical modeling used in simulated annealing and our proposed simulator.

2.1 The Simulated Annealing Algorithm

In the early 1980s Kirkpatrick et al. (1983) and independently Cemy (1985)[7] introduced the concepts of annealing in combinatorial optimization. Originally these concepts were heavily inspired by an analogy between the physical anneahng process of solids and the problem of solving large combinatorial optimization problems. Since this analogy is quite appealing we use it here as a background for introducing simulated annealing. In condensed matter physics, anneahng is known as a thermal process for obtaining low energy states of a sohd in a heat bath. The process consists of the following two steps:

- increase the temperature of the heat bath to a maximum value at which the solid melts;
- decrease carefully the temperature of the heat bath until the particles arrange themselves in the ground state of the solid.

In the liquid phase, all particles arrange themselves randomly, whereas in the ground state of the solid, the particles are arranged in a highly structured lattice, for which the corresponding energy is minimal. The ground state of the solid is obtained only if the maximum value of the temperature is sufficiently high and the cooling is performed sufficiently slowly. Otherwise, the solid will be frozen into a meta-stable state rather than into the true ground state. Metropolis et al.[7] introduced a simple algorithm for simulating the evolution of a solid in a heat bath to thermal equilibrium. Their algorithm is based on Monte Carlo techniques (Binder, 1978) and generates a sequence of states of the solid in the following way.

Given a current state i of the solid with energy E_i , then a subsequent state j is generated by applying a perturbation mechanism which transforms the current state into a next state by a small distortion, for instance by displacement of a particle. The energy of the next state is E_i . If the energy difference, $E_j - E_i$, is less than or equal to zero, the state j is accepted as the current state. If the energy difference is greater than zero, then the state j is accepted with a probability given by

$$\exp\left(\frac{E_i - E_j}{k_B T}\right) \tag{3}$$

where T denotes the temperature of the heat bath and kB is a physical constant called the Boltzmann constant. The acceptance rule described above is known as the Metropolis criterion and the algorithm that goes with it is known as the Metropolis algorithm. It is known that, if the lowering of the temperature is done sufficiently slowly, the solid can reach thermal equilibrium at each temperature. In the Metropohs algorithm this is achieved by generating a large number of transitions at a given value of the temperature. Thermal equilibrium is characterized by the Boltzmann distribution, which gives the probability of the solid of being in a state / with energy Ei at temperature T, and which is given by

$$P_T \left\{ X = i \right\} = \frac{\exp\left(-E_i / k_B T\right)}{\sum \exp\left(-E_i / k_B T\right)}$$
(4)

where X is a random variable denoting the current state of the solid and the summation extends over all possible states. As we indicate below, the Boltzmann distribution plays an essential role in the analysis of the convergence of simulated annealing. Returning to simulated annealing, the Metropolis algorithm can be used to generate a sequence of solutions of a combinatorial optimization problem by assuming the following equivalences between a physical many-particle system and a combinatorial optimization problem:

- solutions in the combinatorial optimization problem are equivalent to states of the physical system;
- the cost of a solution is equivalent to the energy of a state. Furthermore, we introduce a control parameter which plays the role of the temperature. Simulated annealing can thus be viewed as an iteration of Metropolis algorithms, executed at decreasing values of the control parameter.

We can now let go of the physical analogy and formulate simulated annealing in terms of a local search algorithm. To simplify the presentation, we assume, in the remainder of this chapter, that we are dealing with a minimization problem. The discussion easily translates to maximization problems. For an instance (S, f) of a combinatorial optimization problem and a neighborhood function .The meaning of the four functions in the below procedure in fig. 2. is obvious: INITIALIZE computes a start solution and initial values of the parameters c and L; GENERATE selects a solution from the neighborhood of the current solution; CALCULATE.LENGTH and CALCULATE_CONTROL compute new values for the parameters L and c, respectively.

As already mentioned, a typical feature of simulated annealing is that, besides accepting improvements in cost, it also accepts deteriorations to a limited extent. Initially, at large values of c, large deteriorations will be accepted; as c decreases, only smaller deteriorations will be accepted and, finally, as the value of c approaches 0, no deteriorations will be accepted at all.

The below is the simulated annealing algorithm:

procedure SIMULATED ANNEALING; begin INITIALIZE (istart, Co, Lo); k:=0; repeat for / := 1 to L_k do begin GENERATE (j from S_i); i f f(j) \leq f(i) then i := j *else* (f(i) - f(i))

else $\left(\frac{f(i)-f(j)}{c_k}\right)$ random[0, 1) then i := j end; k:= k + 1; CALCULATE_LENGTH (Lk); CALCULATE_CONTROL(ck); until stopcriterion end;

2.2 The Mathematical Model and the proposed simulator Simulated annealing can be mathematically modeled by means of Markov chains. In this model, we view simulated annealing as a process in which a sequence of Markov chains is generated, one for each value of the control parameter. Each chain consists of a sequence of trials, where the outcomes of the trials correspond to solutions of the problem instance.

Let {S, f) be a problem instance, N a neighborhood function, and X(k) a stochastic variable denoting the outcome of the kth trial. Then the transition

probability at the ^th trial for each pair i, $j \in S$ of outcomes is defined as

$$pij(k) = p\{x(k) = j | x(k-1=i)\} = \begin{cases} \left\{G_j\left(c_k A_j\left(c_k\right)\right)f & i \neq j \\ 1 - \sum_{i \in S, l \neq i} \left\{G_j\left(c_k A_j\left(c_k\right)\right)f & i = j \end{cases}\right\} \end{cases}$$

where G_{ij} (ck) denotes the generation probability, i.e. the probability of generating a solution j when being at solution i, and G_{ij} (ck) denotes the acceptance probability, i.e. the probability of accepting solution j, once it is generated from solution i. The most frequently used choice for these probabilities is the

following : G_a(ck) =

$$\begin{cases} \left| N(i) \right|^{-1} & if \ j \in S_i \\ 0 & if \ j \notin S_i \end{cases}$$

$$\begin{array}{l} \text{And} \\ \text{Aj(ck)} = \\ \begin{cases} 1 & f \ f(j) \leq f(i) \\ \exp((f(i) - f(j) / c) & f \ f(j) > f(i) \end{cases}$$

$$\begin{array}{l} \text{(6)} \end{cases}$$

For fixed values of c, the probabilities do not depend on k, in which case the resulting Markov chain is time-independent or homogeneous. Using the theory of Markov chains it is fairly straightforward to show that, under the condition that the neighborhoods are strongly connected—in which case the Markov chain is irreducible and periodic—there exist a unique stationary distribution of the outcomes. This distribution is the probability distribution of the solutions after an infinite number of trials.

The following is the Single-Layer or Raster CNN simulation with Simulated Annealing: Algorithm:

(Single-Layer or Raster CNN simulation with Simulated Annealing) Obtain the input image, initial conditions and templates from user; /* M,N = # of rows/columns of the image */

/* APPLY SIMULATED ANNEALING */ begin INITIALIZE (istart, Co, Lo); k:=0; repeat for i := 1 to L, do begin GENERATE (j from S.); $i f f(j) \leq f(i)$ then i := jelse $\left(\frac{f(i)-f(j)}{c_k}\right)$ > random[0, 1) then i := j end; k:= k + 1; CALCULATE_LENGTH (Lk); CALCULATE_CONTROL(ck); until stopcriterion end: /* Use the optimized parameters from the simulated annealing */ while (converged-cells < total # of cells) (for (i=l; i<=M; i++) for (j=l; j<=N; j++) (if (convergence-flag[i] [i I) /* calculation of the next state*/ continue; /* current cell already converged */

$$\boldsymbol{\chi}_{ij}(\boldsymbol{t}_{n+1}) = \boldsymbol{\chi}_{ij}(\boldsymbol{t}_n) + \int_{\boldsymbol{t}}^{n+1} \mathbf{f}^{(n)}(\mathbf{x}(n\tau)) d\mathbf{n}\tau$$

/* convergence criteria */

$$\begin{cases} \\ y \left(\frac{dx_{i}}{dt} - c_{and} y_{u} - \pm i \forall C(k,l) \in N_{i}(k,l) \right) \\ \\ \\ convergence-flag[i][j] = 1; \\ converged-cells++; \\ \\ \} \\ /^{*} end for */ \\ /^{*} update the state values of the whole image*/ \\ for (i=l; i<=M; i++) \\ for (j=l; i<=M; j++) (\\ if (convergence-flag[i][j]) continue; \\ X_{ij}(t_{n+1}) = X_{ij}(t_{n}); \\ \end{cases}$$

#_of_iteration++;

) /* end while */

The raster approach implies that each pixel is mapped onto a CNN processor. That is, we have an image processing function in the spatial domain that can be expressed as:

$$g(x,y) = T(f(x,y))$$

(7)

where f(.) is the input image, g(.) the processed image, and T is an operator on f(.) defined over the neighborhood of (x,y).

3 Numerical Integration Methods

Three of the single-step numerical integration algorithms used in the CNN behavioral simulator described here. They are RK4(2), RK4(3), and RK6(4) algorithms.

3.1.1 Stepsize selection algorithm.

There are currently two widely used methods that have appeared in the literature for changing the stepsize of p (q)-order RK codes. The first is to apply the formula (see [9])

$$h_{eq} = f_i \left(\frac{TOL}{EST_n} \right)^{\frac{1}{r-1}}$$
(8)

Where f₁ is a safety factor and the new sought-after stepsize

 $h_{_{n+1}}$ = $x_{_{n+1}}$ - $x_{_n}$ is predicted in terms of an estimate of the local error EST_n which is based on the approximation

(9)

$$EST_n \approx \mathcal{Y}_n - \mathcal{Y}_n$$

Assuming \mathcal{Y}_{*} , \mathcal{Y}_{n} to be the pth-, qth-order approximate solutions, respectively, at the previous grid point xn and TOL the requested tolerance. If

$$EST_n \leq TOL$$

Then the computed solution yn+1 is accepted and the integration is carried out, otherwise(5) is reevaluated by substituting

$$EST_n \rightarrow EST_{n+1}$$

This methodology is termed the error per step (EPS) mode (see Shampine [10]).

An alternative is to consider the same algorithm (5), but to use, instead of (6), the approximation

$$EST_{n} \cong \frac{\mathcal{Y}_{n} - \mathcal{Y}_{n}}{h_{n}}, \qquad (10)$$

This is called error per unit step (EPUS) [10].

3.1.2 RK4(2) and RK4(3) at n = 4

According to [8], The equations of RK4(2) and RK4(3) are:

$$\begin{split} & \mathcal{V}_1 = \mathrm{sf}(\mathrm{tot}(\mathrm{sf})) \\ & \mathcal{V}_1 = \mathrm{sf}(\mathrm{tot}(\mathrm{sf})) + \frac{5}{14} - \mathcal{V}_1 \\ & \frac{52}{14} - \mathcal{V}_1 \\ & \mathcal{V}_1 = \mathrm{sf}(\mathrm{tot}(\mathrm{sf})) + \frac{505}{14} - \mathcal{V}_1 - \frac{116}{1216} - \mathcal{V}_1 \\ & \mathcal{V}_1 = \mathrm{sf}(\mathrm{sf}(\mathrm{sf})) + \frac{2556}{142} - \mathcal{V}_2 \\ & -\frac{1089}{108} - \mathcal{V}_2 \\ & + \frac{10}{949} - \mathcal{V}_2 \\ & \mathcal{V}_1 = \mathrm{sf}(\mathrm{sf}(\mathrm{sf})) + \frac{19}{116} - \mathcal{V}_1 + \frac{343}{1214} - \mathcal{V}_1 \\ & -\frac{1331}{1159} - \frac{73}{\mathcal{V}_1} - \frac{73}{448} - \mathcal{V}_1 \end{split}$$

Therefore, the final integration is a weighted sum of the five calculated derivates is given:

$$\begin{array}{rcrr} x_{ij}((n+1)\tau) &= x_{ij}(n\tau) &+ & \hline 19 & & & 120\\ x_{ij}((n+1)\tau) &= x_{ij}(n\tau) &+ & \hline 130 & k^1_{ij} &+ & \hline 990 & k^2_{ij}\\ &+ & \hline 1331 & & & & \\ + & \hline 3159 & k^3_{ij} + & \hline 486 & k^4_{ij} & (11) \end{array}$$

The difference between Rk4(2) and RK4(3) is the local truncation error in the case of RK4(2) is given by using the RK(2) i.e.

 $\frac{4}{y_{ij}(n+1)\tau} = y_{ij}(n\tau) + \frac{4}{55} k_{ij}^{1} + \frac{343}{1215} k_{ij}^{2}$ $+ \frac{13}{18} k_{ij}^{3} (12)$

But local truncation error in the case of RK4(3) is given by using the RK(3)i.e.

$$\begin{array}{c} \displaystyle \frac{11}{130} & \frac{637}{k^3_{e}} \\ \displaystyle + \frac{605}{3159} & k^3_{e} \end{array} , \begin{array}{c} \displaystyle \frac{73}{1215} & k^3_{e} \end{array}$$

3.1.3 RK8(6) at n= 6 According to [2], The equations of RK 8(6) are:

$$\begin{split} k^{i}{}_{ij} &= \tau f'(x_{ij}(n\tau)) \\ k^{2}{}_{ij} &= \tau f'(x_{ij}(n\tau)) + \frac{9}{142} k^{i}{}_{ij} \\ \frac{178422123}{k^{3}{}_{ij} &= \tau f''_{i}(x_{ij}(n\tau)) + \frac{178422123}{9178574137} k^{i}{}_{ij} + \end{split}$$

685501333 8224473205 k²a

12257 12257	
$k_{i_0}^{i_0} = \tau f'_{(x_{ij}(n\tau))} + \overline{317988} k_{i_0}^{i_0} + \overline{105996} k_{i_0}^{i_0}$	
2584949729	
$k_{\mu}^{3} = \tau f'(x_{\mu}(n\tau)) + 6554704252 k_{\mu}^{3} -$	
9163901916 2622205779 4	
6184003973 k3, +1777642190 7 k4,	
4418011	
$k_{n}^{4} = \tau f'(x_{n}(n\tau)) - \frac{1}{96055225} k_{n}^{4} + \frac{1}{2}$	
2947922107 3229973413	
1268738173 6 14 1723496041 4 1.5	
2875130530	
12	
$\mathbf{k}_{ij} = \pi_{ij} (x_{ij}(nt)) - 47377207054 \mathbf{k}_{ij} +$	
2702377211 135707089	
$24084535832 \ k^{4}_{ij}$ _ $4042230341 \ k^{5}_{ij}$ +	
299874140	
17933325691 k ⁶ ii	
7872176137	
$k^{s_{ii}} = \tau f'(x_{ii}(n\tau)) - \overline{5003514694} k^{l_{ii}}$	
35136108789 114433184681	
26684798878 k_{4a}^{4a} 9760995895 k_{5a}^{5a} +	
299204996517 254	
$\frac{1}{32851421233}$ $\mathbf{t} \cdot 0 + \frac{39}{39}$ \mathbf{t}^{7}	
3559950777	
7399971898 1-1	
$\mathbf{x}_{ij} = tr(\mathbf{x}_{ij}(nt)) - 757577050 \mathbf{x}_{ij} - 20200201521 - 42434013370$	
4405504148 14 9366905709 15	
12051107050	
200428/1/00 1295119/030	
$5300635453 k_{ij}^{\circ} + 1499985011 k_{ij}^{\circ} +$	
59527523	
$6331620793 k_{ij}^{s}$	
9106702590	
10570705091	
$\frac{k^{10}}{k^{10}} = \tau t^{0}(x_{ij}(n\tau)) - 10570793981 k^{1}_{ij} - 106277106011$	
46181454005 1962//106011	
$\frac{57}{51227}$ $k_{ij}^{4} = \frac{291}{9424052}$ $k_{ij}^{5} + \frac{6255125242}{100}$	
<u>635/5135343</u> <u>9348448139</u> <u>957946776</u>	
$11491808333 k_{ij}^{6} + 85/846/76 k_{ij}^{7} +$	
<u>195434294</u> <u>617468037</u>	
$9727139945 k_{ij}^{s} = 15757346105 k_{ij}^{9}$	
6373809055	
$k_{ij}^{11} = \tau f(x_{ij}(n\tau)) - 5357779452 k_{ij}^{1}$	
<u>150772749657</u> <u>58076657383</u>	
21151088080 k_{ij}^{4} - 6089469394 k_{ij}^{5} +	
9252721190 132381309631	
1221566797 k_{ij}^{6} + 11748965576 k_{ij}^{7} +	
704633904 656417033	
13813696331 k^{8}_{ij} + 8185349658 k^{9}_{ij} -	
1669806516	
10555289849 k ¹⁰ ij	

	2726346953	
$\underline{k}^{12}_{ij} = \tau f'(x_{ij}(n\tau))$	6954959789 k ¹ _{ij}	+
24906446731	65277767625	
6359105161 k ⁴ _{ij}	23298960463 k ⁵ ij	+
39128152317	40638357893	
16028215273 k ⁶ _{ij}	_ 16804059016 k ⁷ ij	+
7437361171	1040125706	
21911114743 k ^s ij	+ 5334949109 k ⁹ ij	
1129865134	6253441118	
- 5812907645 k ¹⁰ _{ij}	+ $\overline{10543852725} k^{11}_{ij}$	

Therefore, the final integration is a weighted sum of the twelve calculated derivates is given:

438853193	
$x_{ij}((n+1)\tau) = x_{ij}(n\tau) + \overline{9881496838} k_{ij}^{1}$	+
11093525429 481311443	
$\overline{31342013414}$ k^{6}_{ij} + $\overline{1936695762}$ k^{7}_{ij}	-
3375294558 9830993862	
$\overline{10145424253}_{k_{ij}^{s}+} \overline{5116981057}_{k_{ij}^{9}}$	
138630849943	
50747474617 k ¹⁰ ij	
7152278206	
$+ 5104393345 k^{11}{}_{ij}$ (14)	

Where f(l.) is computed according to (1). There are many single step methods available to us for this purpose. But, one option worth considering is the combination of two methods in solving for the solution. So we use Rk8(6) to make a very efficient computer solving the problem the way it evaluates the integral presented

method	Mean Square Error	Peak Signal to Noise Ratio	MNormalized Cross-Correlation	Average Difference	Structural Content	Maximum Difference	Normalized Absolute Error
RK4(2)	1.6661e+003	12.5551	0.9349	8.9551	1.3255	243	0.0710
RK4(3)	1.6990e+003	11.4449	0.9306	6.1449	1.4010	235	0.0400
RK8(6)	1.6603e+003	10.4044	0.9121	6.5556	1.7990	236	0.0300

4 Simulation Results and Comparisons

The simulation time used for comparisons is the actual CPU time used. The input image format for this simulator is a JPEG format.





Fig.2. Image processing (a) After Averaging Template (b) After Averaging and Edge Detection

Fig. 2 shows results of the raster simulator obtained from a complex image of 65,536(256x256) pixels. For this example an Averaging template followed by an Edge Detection template were applied to the original image to yield the images displayed in Figs.



Edge Detection Averaging Connected Component

Fig.4. Maximum step size that still yield

convergence for 4 different templates 2a and 2b, respectively.

Also in figure 3, it has been shown the quality measures of the two pictures in 2a and 2b by using the numerical techniques RK4(2),RK4(3) and RK6(4) using simulated annealing. We notice that these results are better than those in the literature.

Since speed is one of the main concerns in the simulation, finding the maximum step size that still yields convergence for a template can be helpful in speeding up the system. The speed-up can be achieved by selecting an appropriate Δt for that particular template. Even though the maximum step



Fig.5. Simulation time comparisons for 4 different numerical techniques for four different templates

size may slightly vary from one image to another, the values in Fig.4 still serve as good references. These results were obtained by trial and error over more than 100 simulations On Lena image with small size 43x64(2752 pixels).

The importance of selecting an appropriate Δt can be easily visualized in Fig. 4. If the step size chosen is too small, it might take many iterations, hence longer time, to achieve convergence. On the other hand, if the step size taken is too large, it might not converge at all or it would converge to erroneous steady state values. The results of Fig. 5 were obtained by simulating Lena image of size 43x64(2752 pixels) using an Edge detection template. We notice that the CPU time for our method is better than those in the literature.

5 Conclusion

As researchers are coming up with more and more CNN applications, an efficient and powerful simulator is needed. So we use simulated annealing in optimizing CNN using the numerical integrations, especially using RK6(4) comparing it to the used methods RK4(2) and RK4(3) in the literature for more efficiency. The simulator hereby presented meets the need in six ways: 1) Depending on the accuracy required

for the simulation, the user can choose from three numerical methods to perform the numerical integration, 2) The input image format is JPEG, which is commonly available, 3) The input image can be of any size, allowing simulation of images available in common practices, 4) CPU time of our methods is better than those in the literature, 5), the quality measures of the pictures and the edge detection for our method is better than those in the literature

REFERENCES

[1] M. El-Sayed Wahed and O.H. Abdel wahed (2012). An efficient numerical integration algorithm for Single-Layer Raster Cellular Neural Networks Simulator. the international Journal of the physical sciences(IJPS), December 16th 2012. | [2] L. 0. Chua and L. Yang(1988). "Cellular Neural Networks: Theory & Applications," IEEE Trans. Circuits and Systems, Vol. CAS-35, pp. 1257-1290. | [3] L.O. Chua and T. Roska(1992). "The CNN Universal Machine Part 1: The Architecture", in Int. Workshop on Cellular Neural Networks and their Applications (CNNA), pp. 1-10. | [4] J. A. Nossek, G. Seiler, T. Roska and L. O. Chua (1992). "Cellular Neural Networks and their Applications (CNNA), pp. 1-10. | [4] J. A. Nossek, G. Seiler, T. Roska and L. O. Chua (1992). "Cellular Neural Networks: Theory and Applications (CNNA), pp. 1-10. | [4] J. A. Nossek, G. Seiler, T. Roska and L. O. Chua (1992). "Cellular Neural Networks: Theory and Applications, Vol. 20, pp. 533-553. | [5] J. Varrientos and E. Sanchez-Sinencio(1992). "CelLLSIM: A cellular neural network simulator for the personal computer," in Proc. 35th Midwest Symp. Circuits Systs, pp. 1384-1387. | [6] W. H. Press, B. P. Flannery, S.A. Teukolsky, and W.T.g Vetterling(1986). "Numerical Recipes. The Art of Scientific Computing", Cambridge University Press, New York. | [7] P.J.M. van Laarhoven and E.H.L. Aarts, (1987) Simulated Annealing: Theory and Application. ISBN 90-277-2513-6 | [8] Ch. Tsitouras and S. N. Papakostas(1991) "Cheap Error methods for ordinary di erential equations, SIAM J. Numer. Anal., 9, pp. 603(637. | [10] L. F. Shampine(1986), Some practical Runge-Kutta formulas, Math. Comp., 46, pp. 135(150. | [11] J. C. Butcher, The Numerical Analysis of Ordinary Di_erential Equations, John Wiley and Sons, Chichester, 1987. | [12] E. Hairer, S. P. N'orsett, and G. Wanner, Solving Ordinary Di_erential Equations, 1, 2nd ed., Springer, Berlin, 1993. | [13] S. N. Papakostas, On a class of families of high order Runge-Kutta methods and pairs, 1996, submitted. | [14] S. N. Papakost